

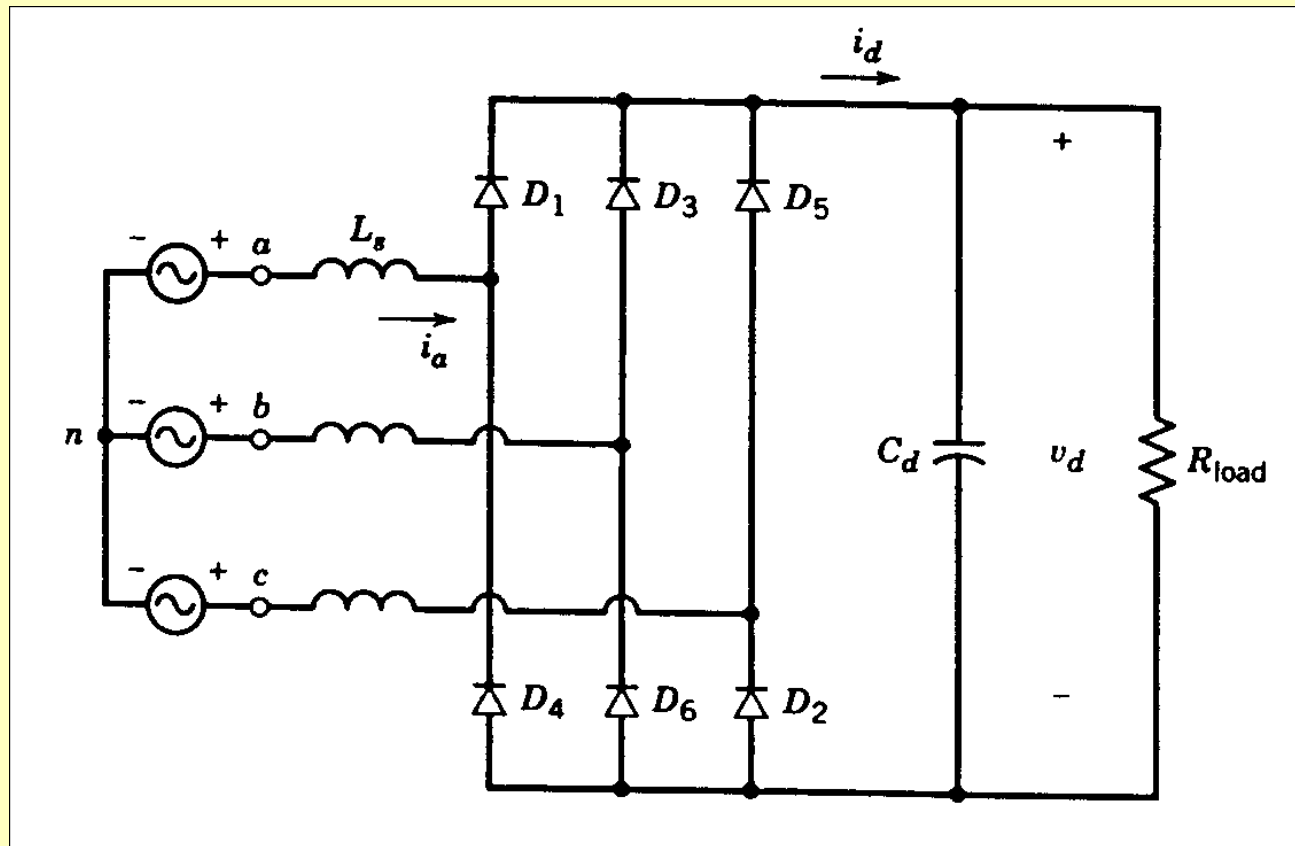
Power converters AC/DC and DC/AC - MM2

Three phase rectifiers

Content MM2

1. Summary from MM1
2. Three phase rectifier ($L_s = 0$)
3. Three phase rectifier ($L_s \neq 0$)
4. Constant DC-link voltage
5. Characteristics
6. Exercises

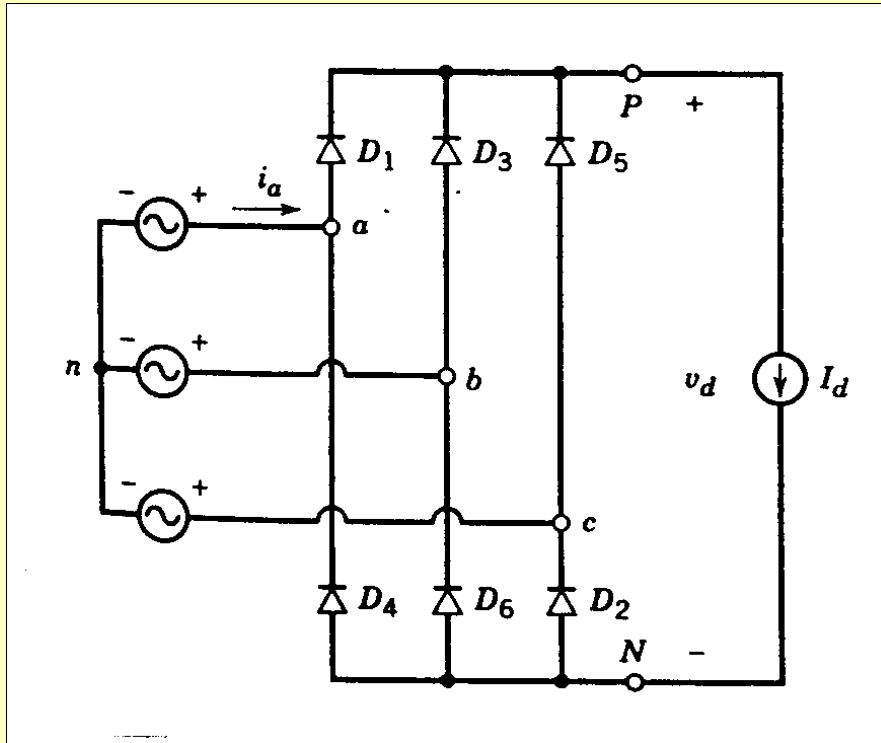
2. Three phase rectifier ($L_s = 0$)



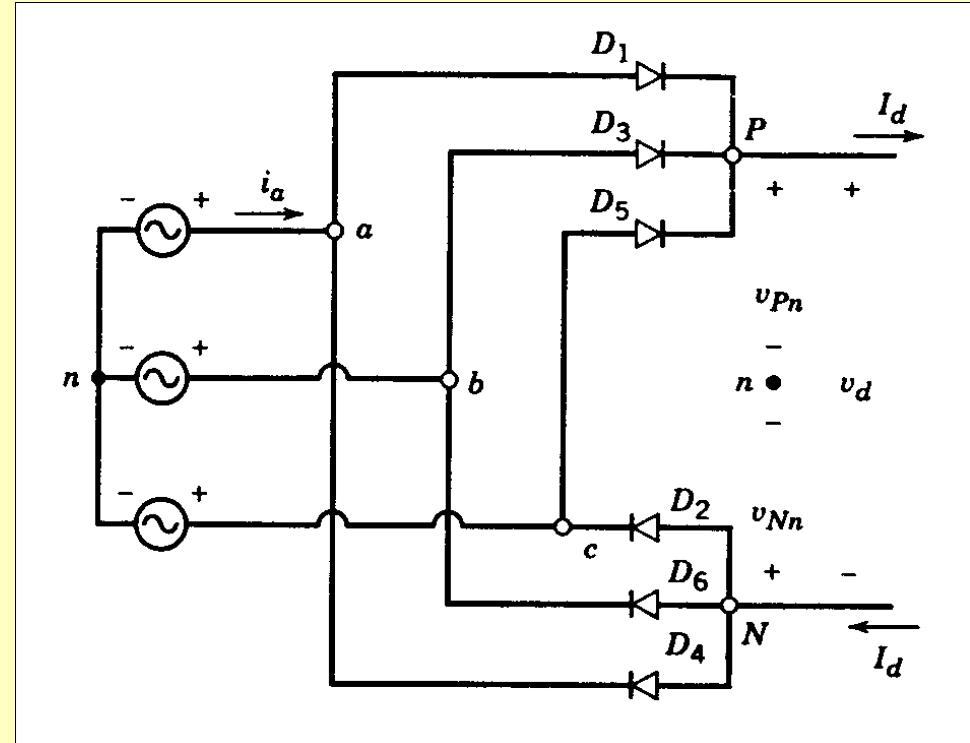
- Three phase line
- Larger power
- Higher voltage (V_d)
- Smaller filter
- Good properties

2. Three phase rectifier ($L_s = 0$)

Constant DC current



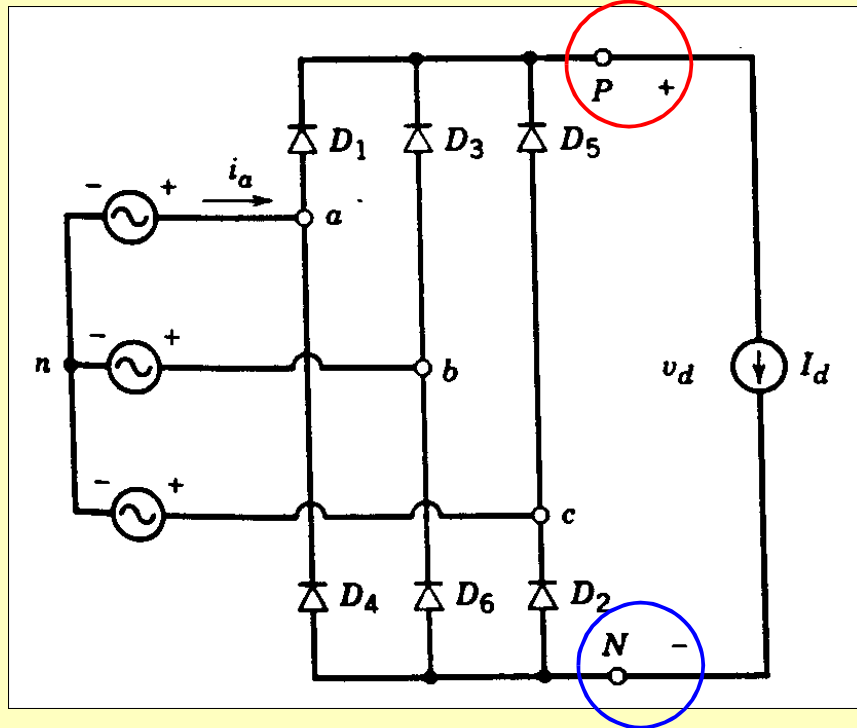
The highest voltage conduct



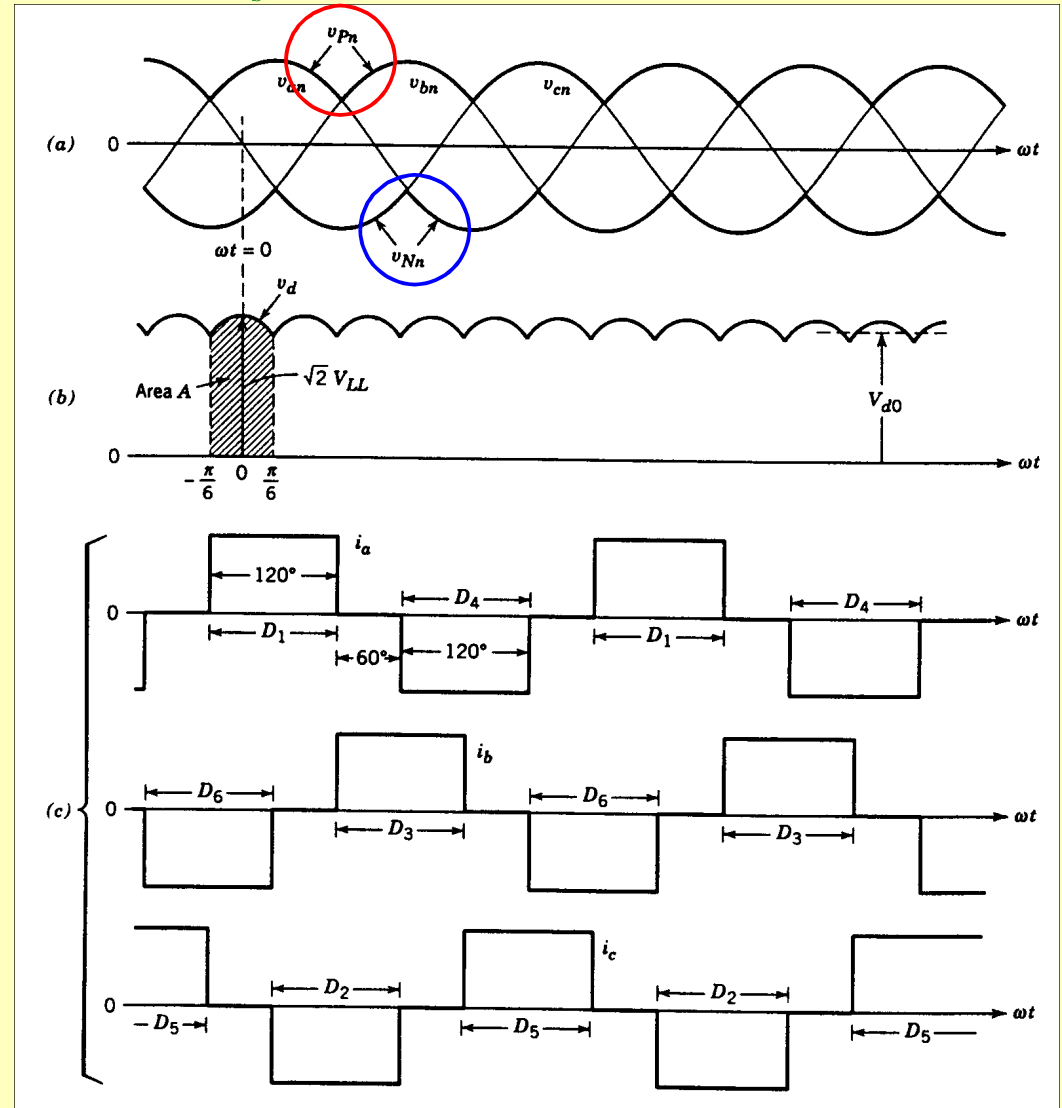
The lowest voltage conduct

2. Three phase rectifier ($L_s = 0$)

Constant DC-current

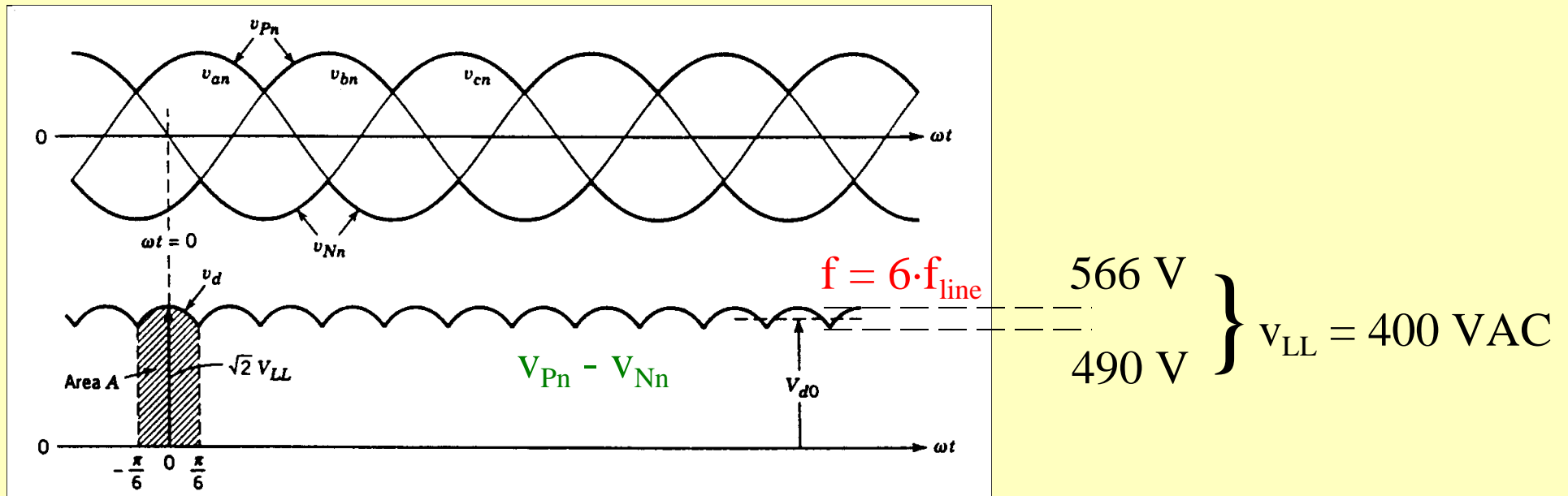


Current with resistive load ?



2. Three phase rectifier ($L_s = 0$)

Current/voltage



DC-link voltage

$$v_d = v_{ab} = \sqrt{2} V_{LL} \cos \omega t \quad -\frac{1}{6}\pi < \omega t < \frac{1}{6}\pi$$

RMS current

$$I_s = \sqrt{\frac{2}{3}} I_d = 0.816 I_d$$

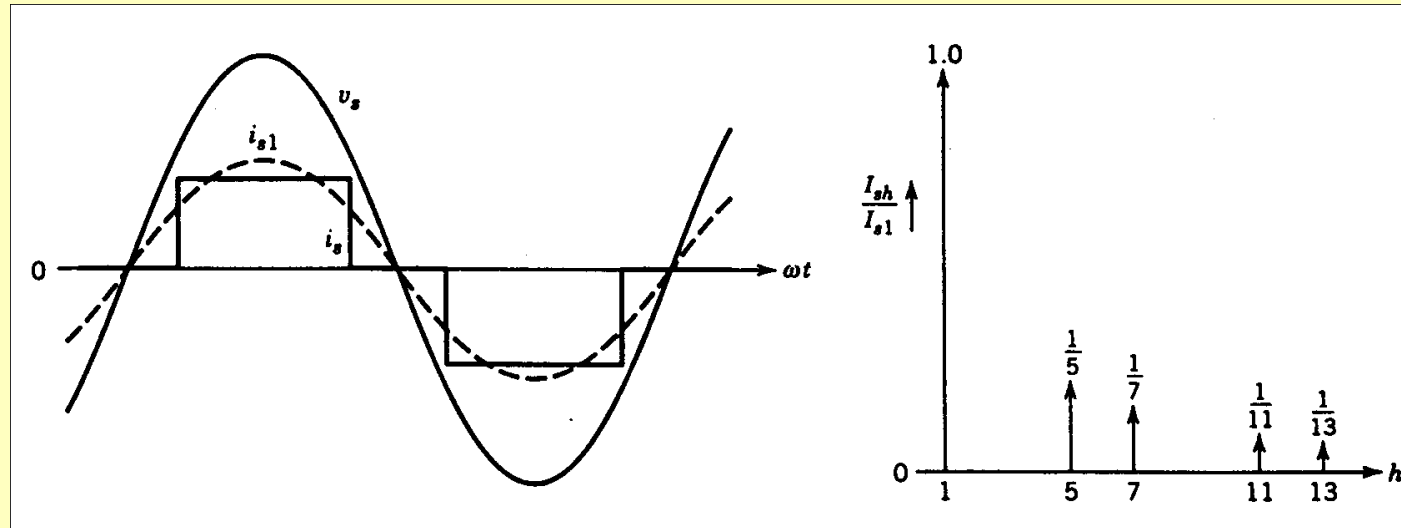
Average voltage

$$V_{d0} = \frac{1}{\pi/3} \int_{-\pi/6}^{\pi/6} \sqrt{2} V_{LL} \cos \omega t d(\omega t) = \frac{3}{\pi} \sqrt{2} V_{LL} = 1.35 V_{LL}$$

$$V_{LL} = 400 \text{ VAC} \Rightarrow V_{d0} = 540 \text{ VDC}$$

2. Three phase rectifier ($L_s = 0$)

Current



1. Harmonic current

$$I_{s1} = \frac{1}{\pi} \sqrt{6} I_d = 0.78 I_d$$

DPF

$$\text{DPF} = 1.0$$

PF

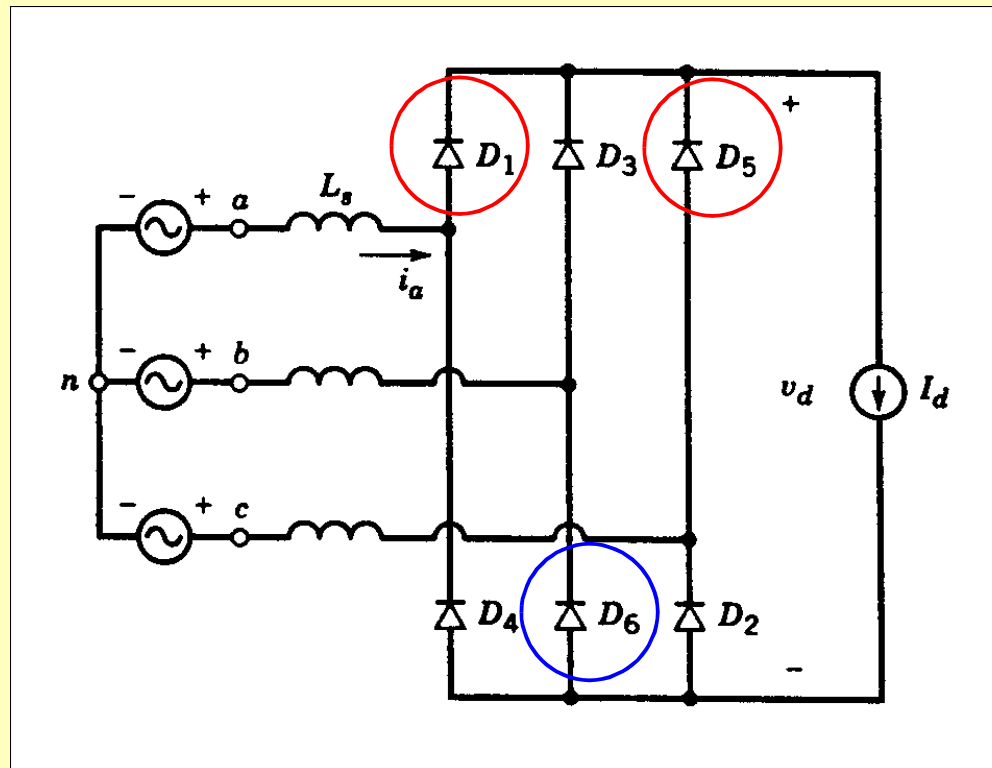
$$\text{PF} = \frac{3}{\pi} = 0.955$$

$$\text{PF} = \text{DPFI}_{s1} \rho_{\text{vore}} I_s = \frac{\frac{1}{\pi} \sqrt{6} I_d}{\sqrt{\frac{2}{3} I_d}}$$

Smaller harmonics than the single phase rectifier (much smaller)

3. Three phase rectifier ($L_s \neq 0$)

Present 3 phase rectifier



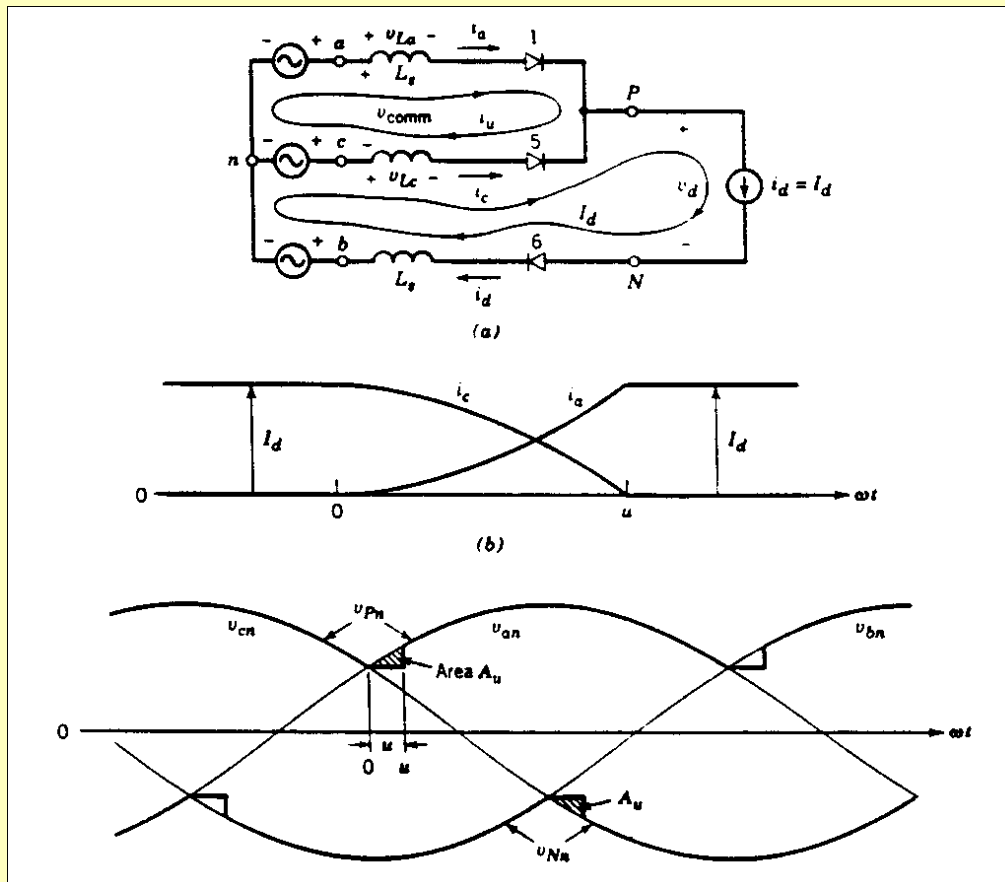
$$D_5 + D_6 \rightarrow D_1 + D_6$$

3 -phase rectifier

- Lower voltage due to voltage drop over L_s

3. Three phase rectifier ($L_s \neq 0$)

Real rectifier



A_u is loss of average DC-link voltage

Inductance voltage

$$v_{La} = L_s \frac{di_a}{dt} = L_s \frac{di_u}{dt}$$

$$v_{Lc} = L_s \frac{di_c}{dt} = -L_s \frac{di_u}{dt}$$

$$v_{comm} = v_{an} - v_{cn} = v_{La} - v_{Lc} = 2L_s \frac{di_u}{dt}$$

$$L_s \frac{di_u}{dt} = \frac{v_{an} - v_{cn}}{2}$$

Commutation interval

$$v_{an} - v_{cn} = \sqrt{2}V_{LL} \sin \omega t$$

$$\omega L_s \int_0^{I_d} di_u = \omega L_s I_d = \frac{\sqrt{2}V_{LL}(1 - \cos u)}{2}$$

$$\cos u = 1 - \frac{2\omega L_s I_d}{\sqrt{2}V_{LL}}$$

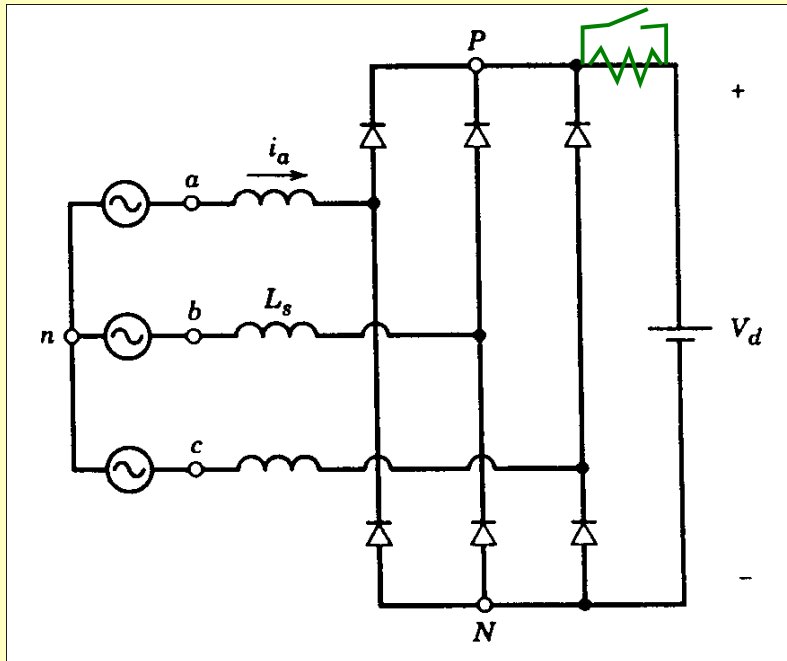
Corrected average DC-link voltage

$$V_d = V_{d0} - \Delta V_d = 1.35V_{LL} - \frac{3}{\pi} \omega L_s I_d$$

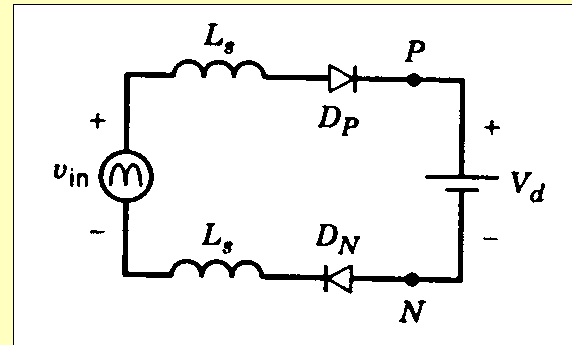
4. Constant DC-link voltage

Dis-continues current

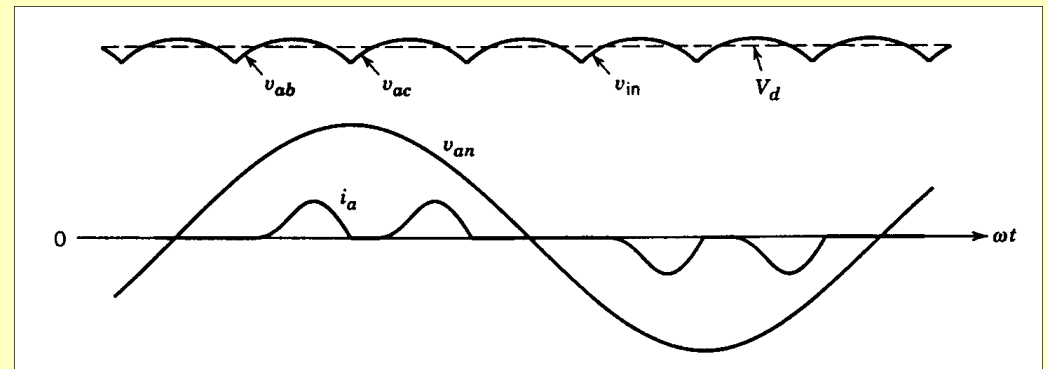
Inrush circuit



Simplified model

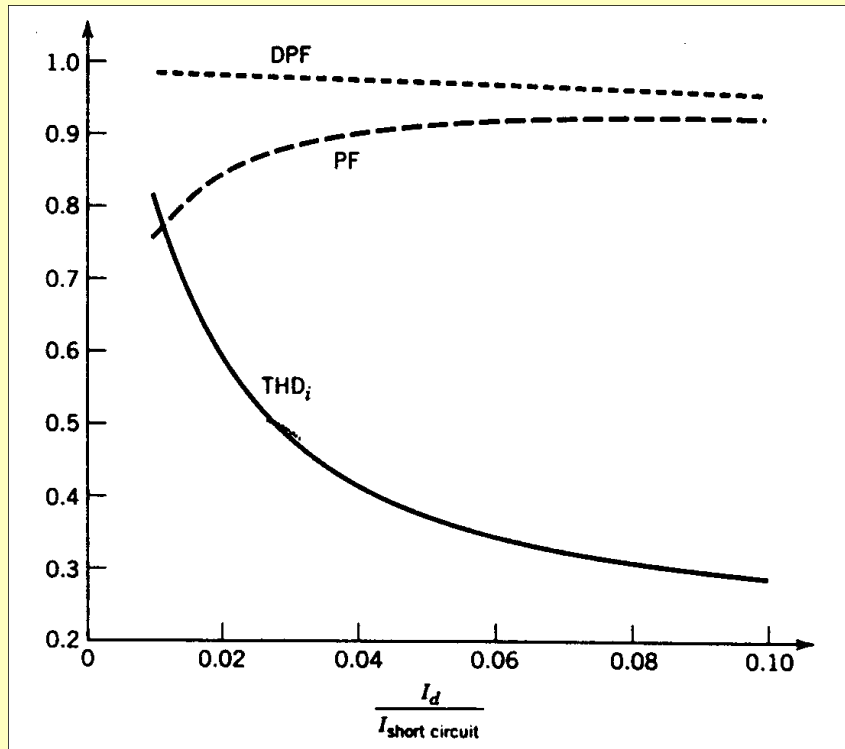


Line current

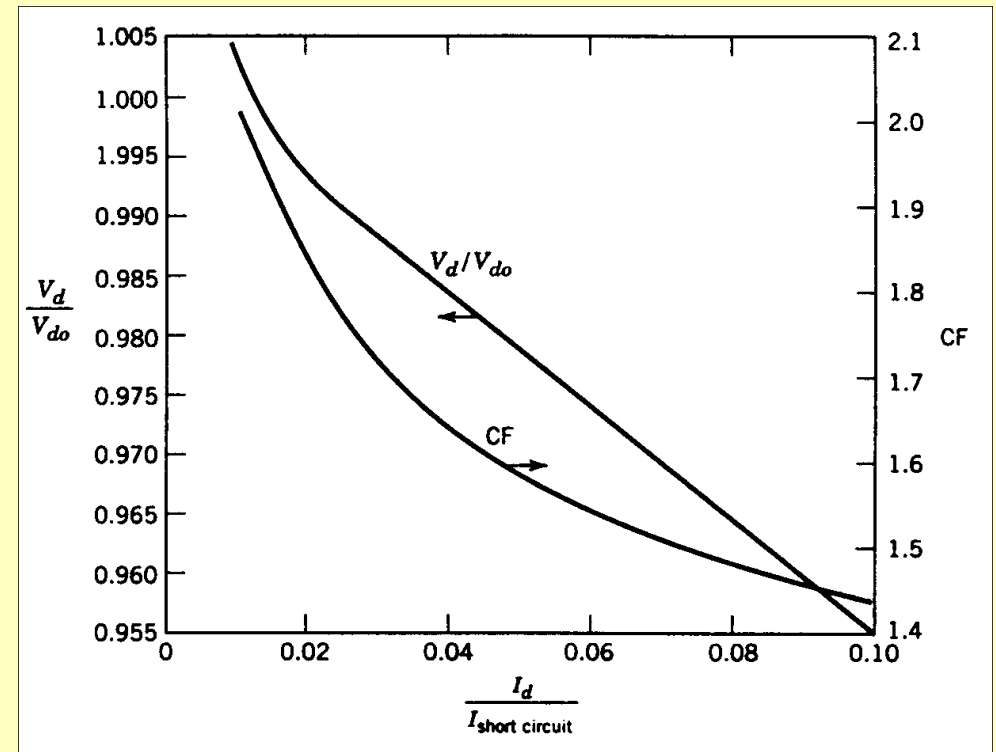


5. Characteristics

DPF, PF, THD_i



Voltage and Crest-factor



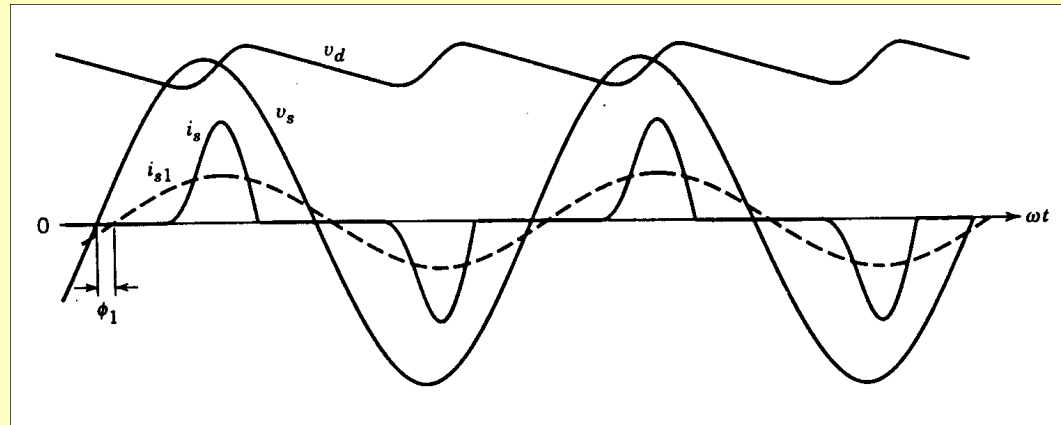
Short circuit current

$$I_{\text{short circuit}} = \frac{V_{LL} / \sqrt{3}}{\omega_1 L_s}$$

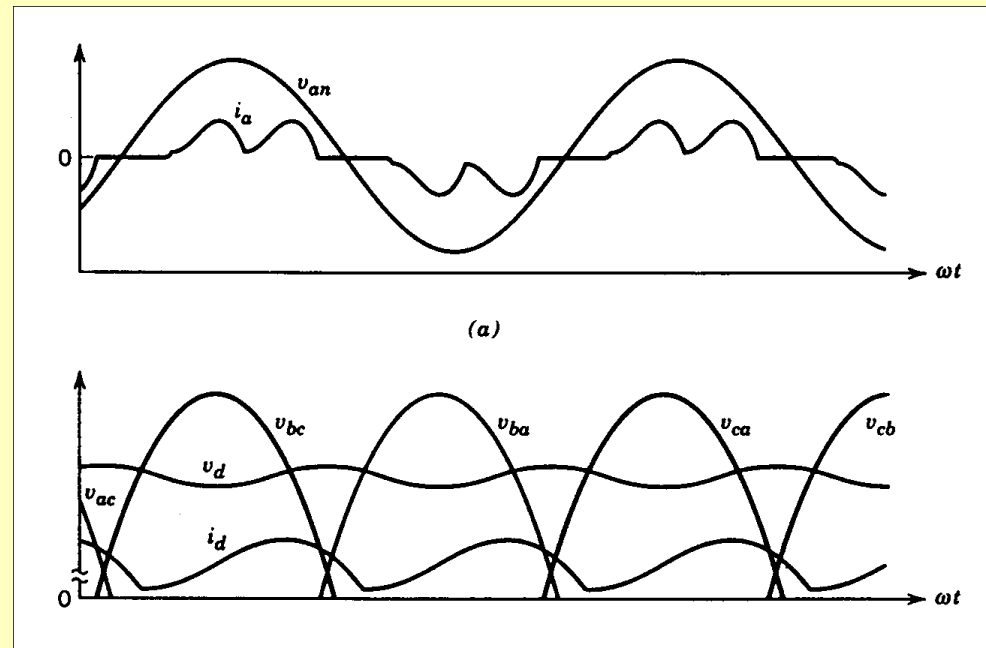
5. Characteristics

Comparison

Single phase



Three phase



6. Exercises

Exercise 7, PSpice-Simulation

Download from www.iet.auc.dk/~por/teaching/power/power.html