

Power converters AC/DC and DC/AC - MM1

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Content MM1

1. Presentation
2. Purpose and content
3. Rectifier principles
4. Single phase rectifier
5. Commutation
6. Constant DC-link voltage
7. Characteristics
8. Exercises

2. Purpose and content

Purpose

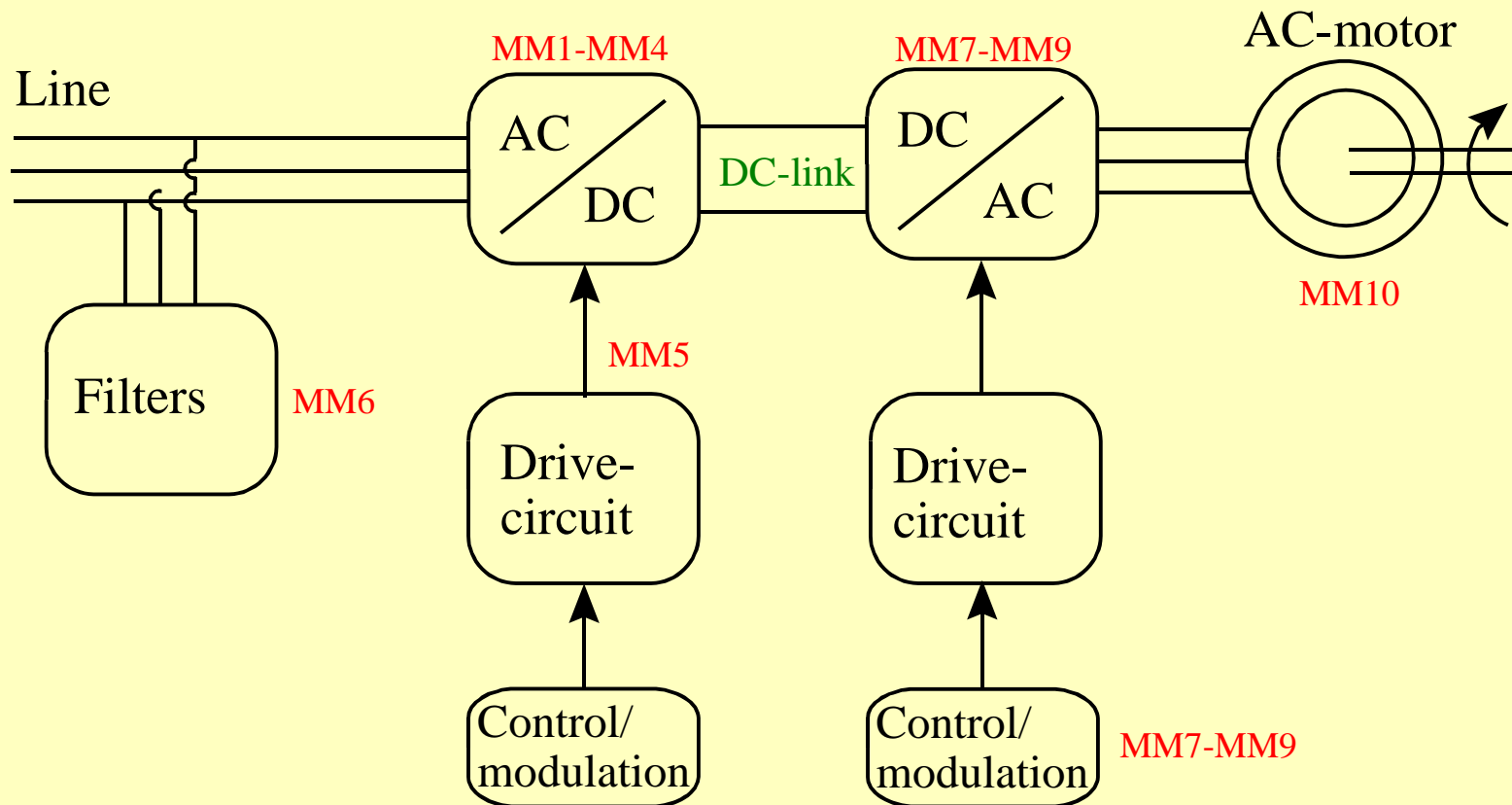
- To understand single- and three-phase AC/DC and DC/AC power conversion
- Design aspects about single and three phase converters

Main content

MM1-MM2	Single- and three-phase AC/DC converters	POR
MM3-MM4	Single- and three-phase AC/DC and DC/AC Thyristor converters	POR
MM5	Thyristors operation mode	POR
MM6	Filters (power)	POR
MM7-MM9	DC/AC conversion with high switching frequency	SMN
MM10	Interaction with electrical motors	SMN

2. Purpose and content

Example : A drive system



2. Purpose and content

More goals

- To use the content of the course in the project
- Get more experience with circuit-simulation tools (P-Spice)
- More experience with power electronics

The form of the course

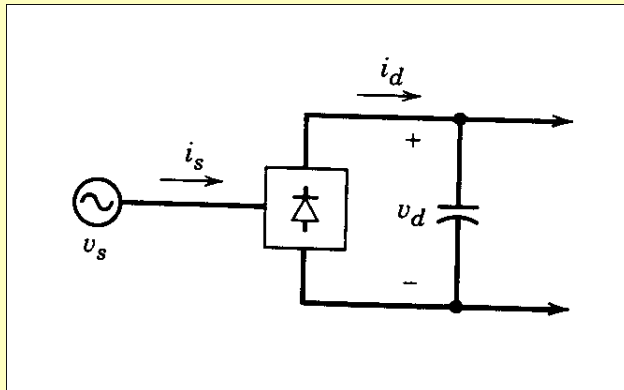
- 2 times lectures of 45 min. per. Mini-Module (MM)
- Exercises
- I expect that the material to each MM are read.
- Primary overheads
- Feedback from you !!. This is very important (Don't be afraid to put questions)
- Course home-page with overheads, exercises and latest information

Course Home-page

<http://www.iet.auc.dk/~por/teaching/power/power.html>

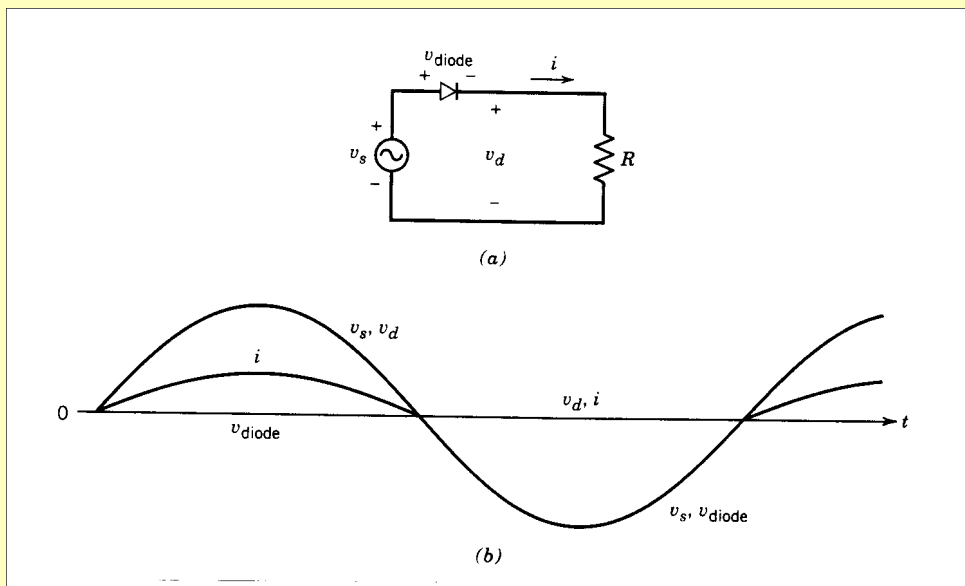
AC/DC

3. Rectifier principles



- DC-voltage
- Load depend
- Current from the grid
- Power supplies
- Drive systems etc.

Resistive Load

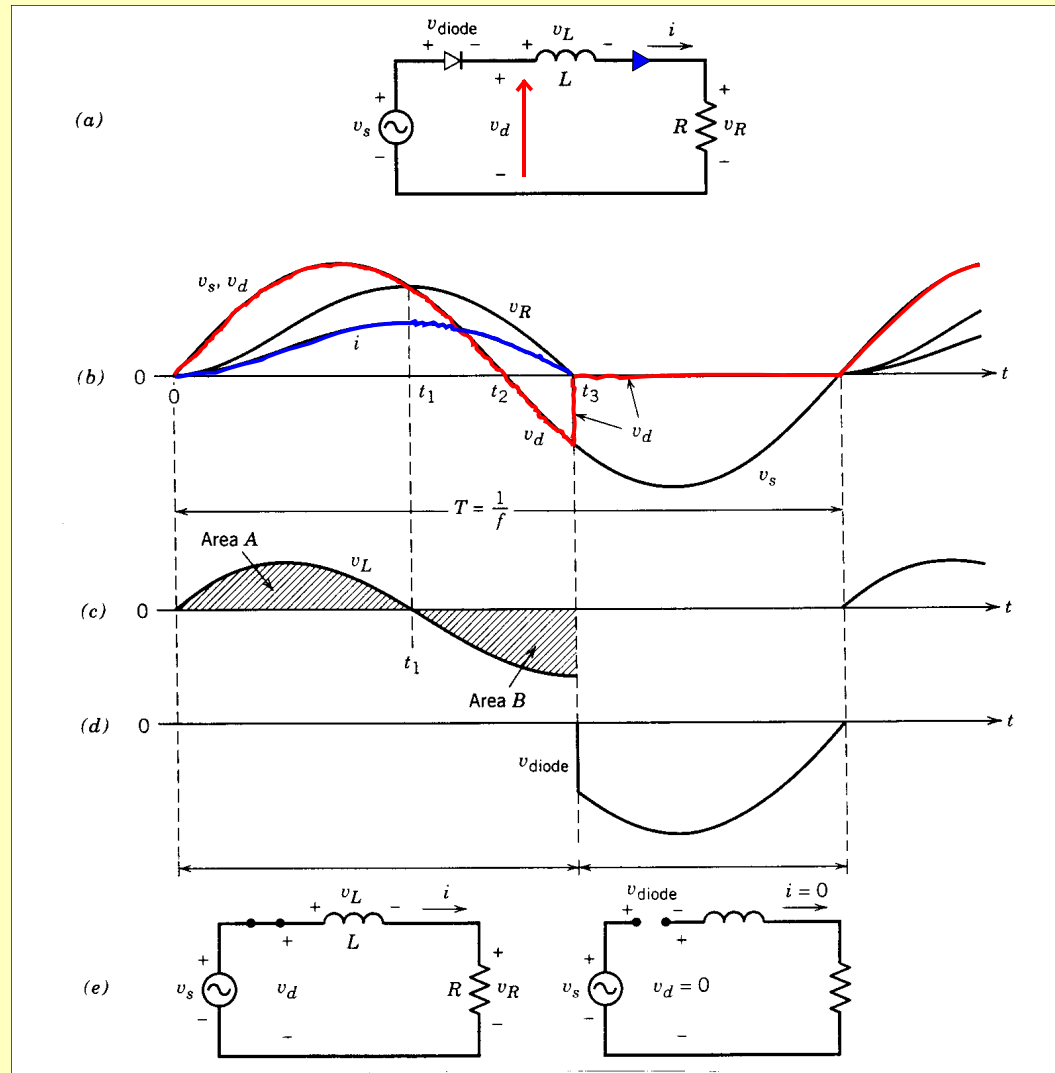


$$V_{\text{diode}} > 0 \Rightarrow \text{Current}$$

$$V_{\text{diode}} < 0 \Rightarrow 0$$

Inductive load

3. Rectifier principles



Basic rules used in power electronics

$$u = L \frac{di}{dt}$$

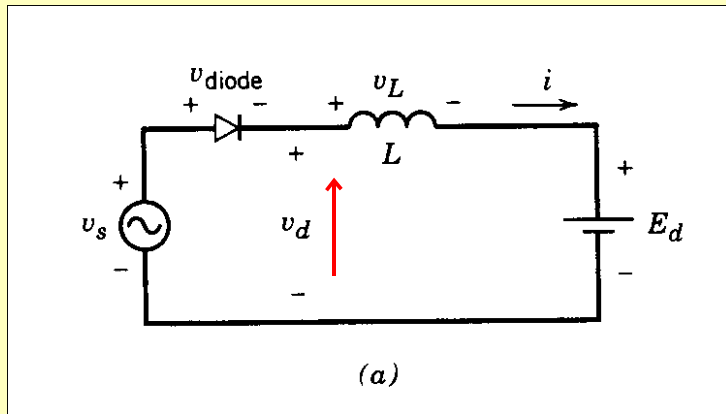
$$\text{Steady-state} : \int_0^T u dt = 0$$

$$i = C \frac{du}{dt}$$

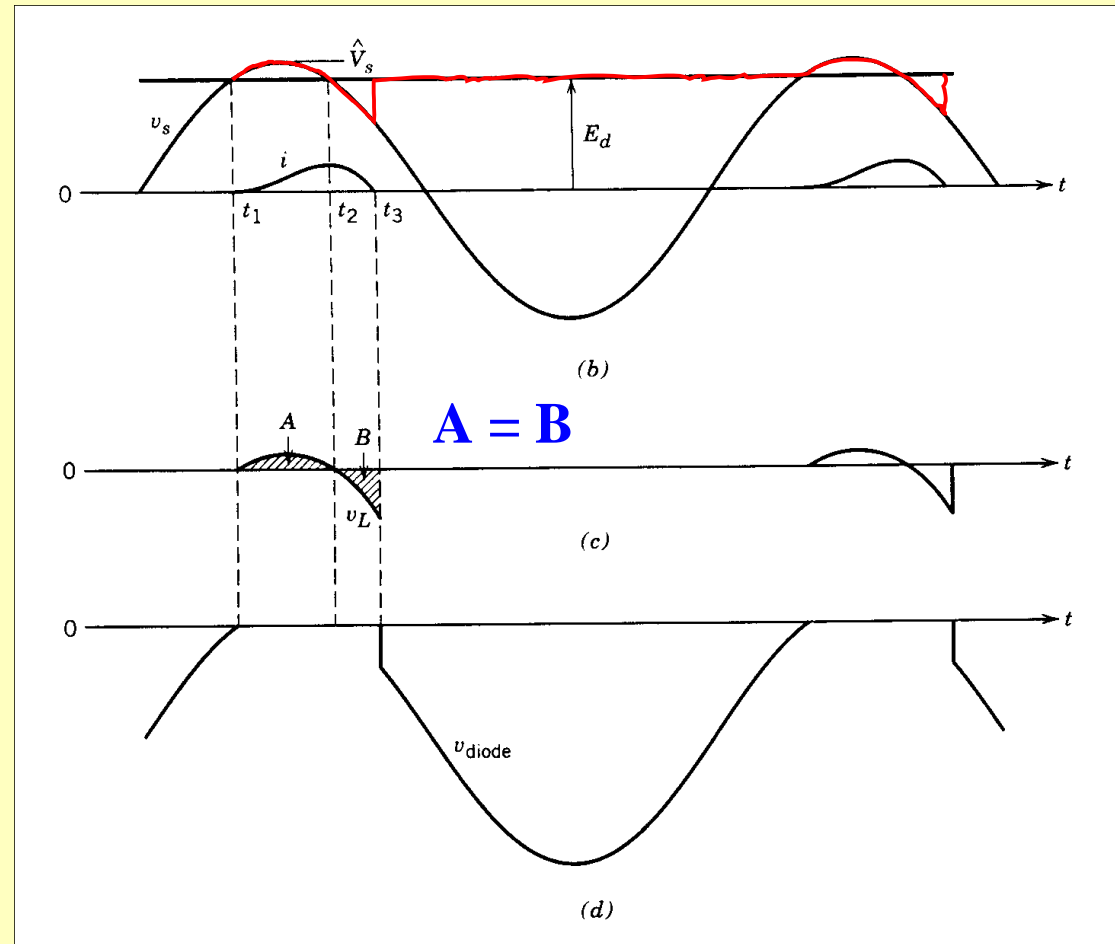
$$\text{Steady-state} : \int_0^T i dt = 0$$

3. Rectifier principles

Internal DC voltage E

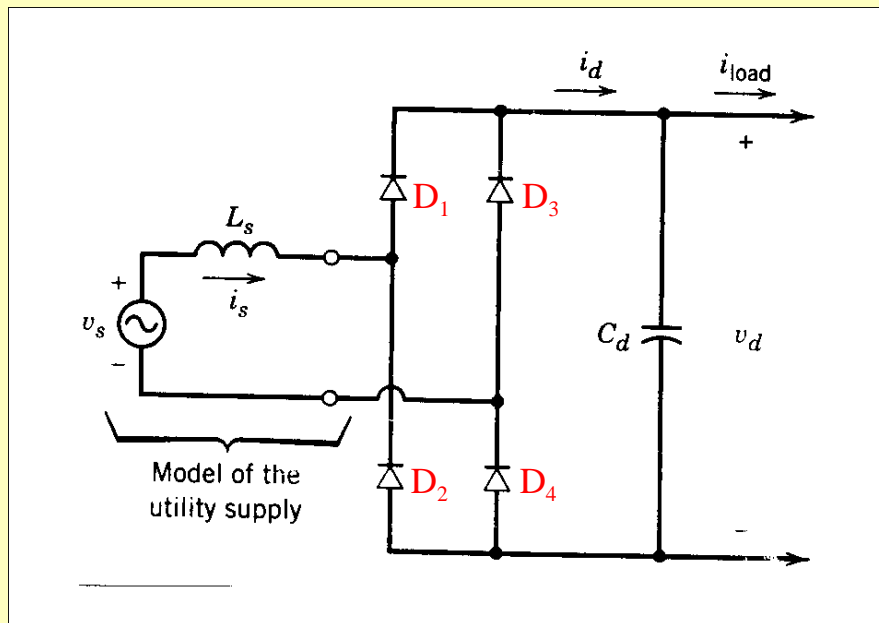


- Capacitor
- Batteries
- DC-motors



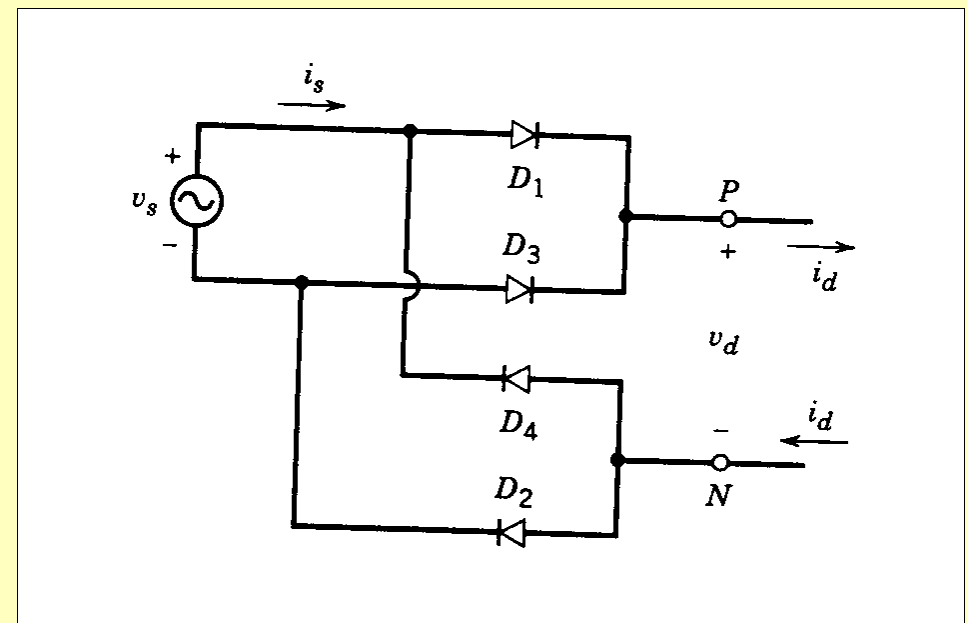
4. Single phase rectifier

Real rectifier



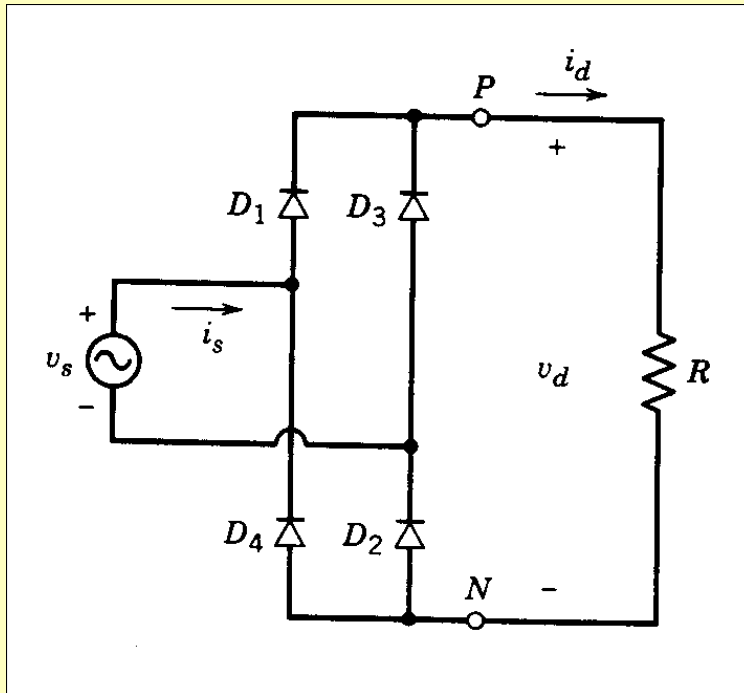
L_s is a model of the line. Typical very dominating in relation to R .

Ideal rectifier

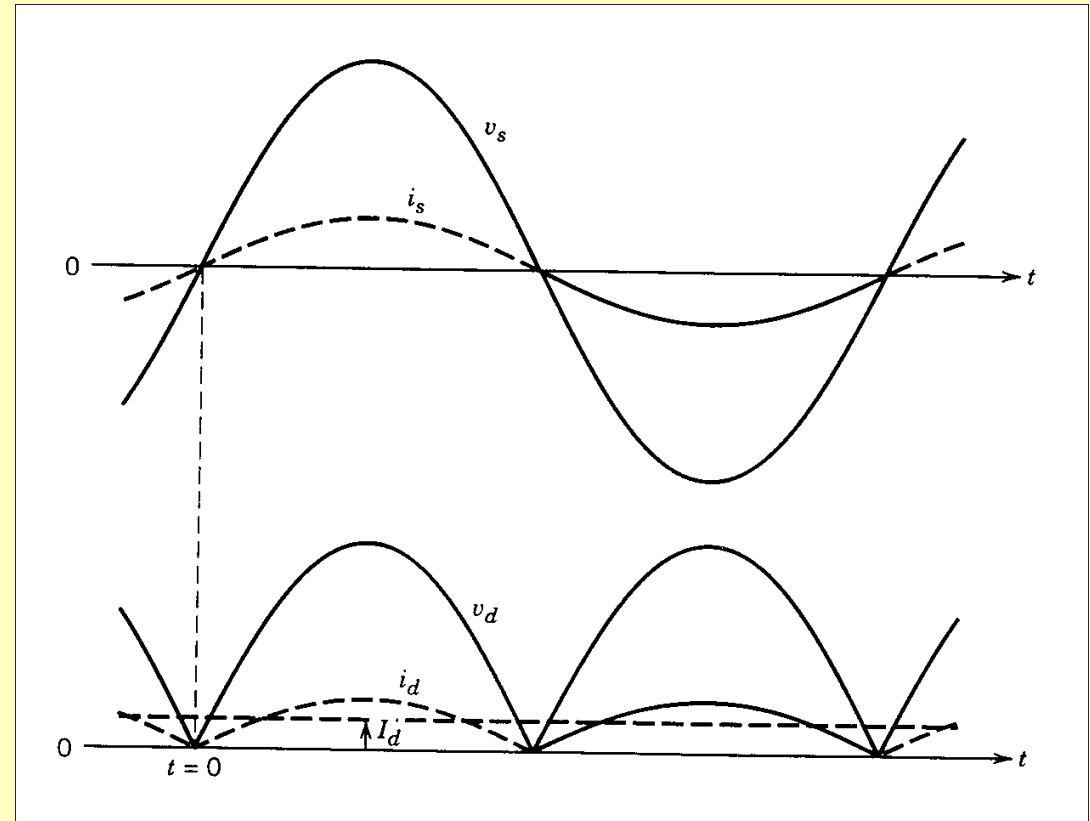


4. Single phase rectifier

Resistive load



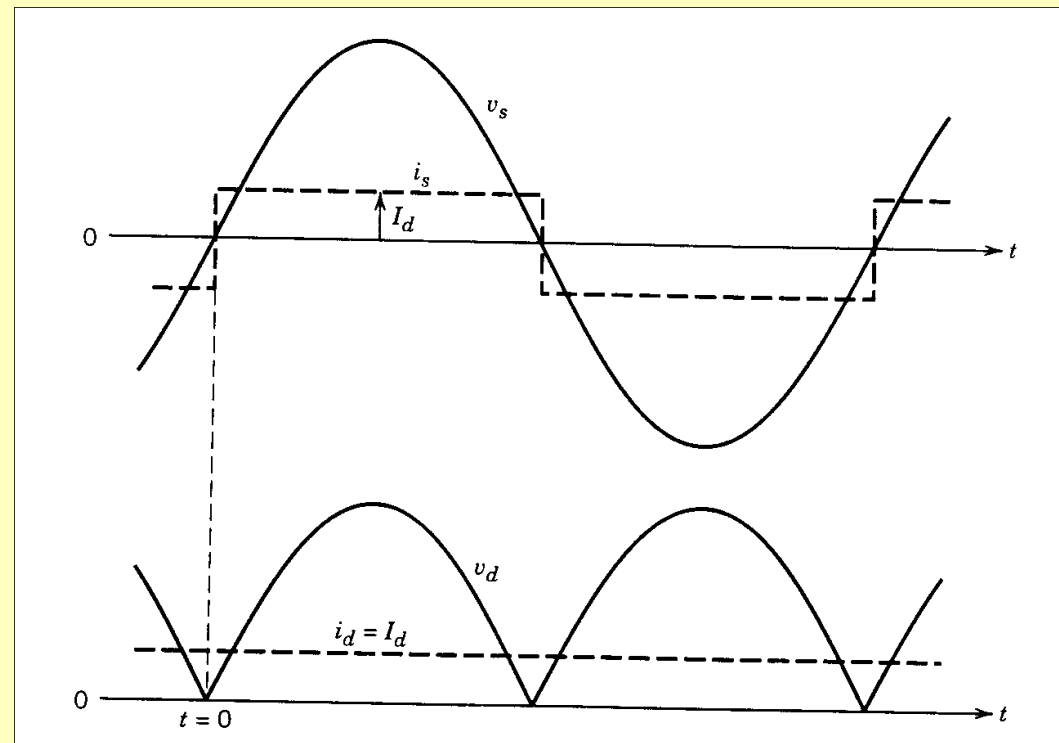
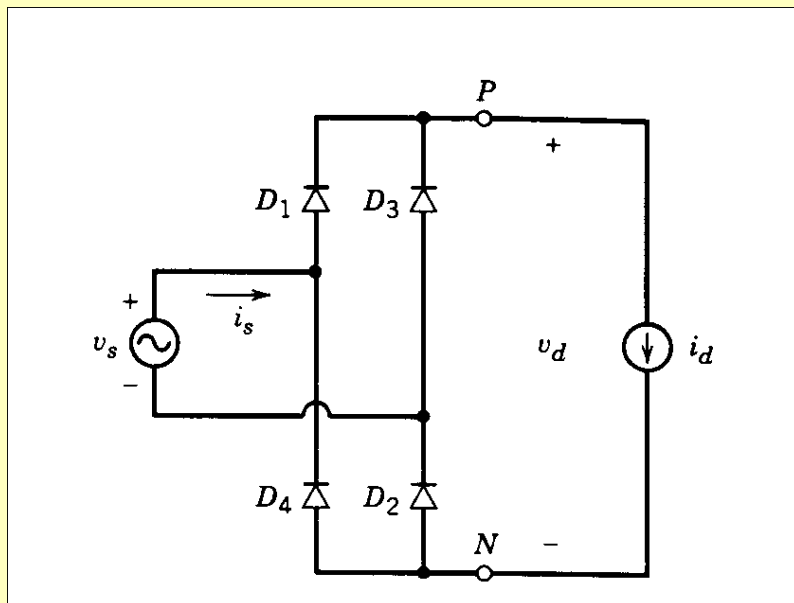
$$L_s = 0$$



$$I_d = \int_0^T i_d dt$$

4. Single phase rectifier

Constant current load (Large inductance)



Average voltage

$$V_{d0} = \frac{2}{\pi} \sqrt{2} V_s \approx 0.9 V_s$$

4. Single phase rectifier

Definitions

Total Harmonic distortion

$$\begin{aligned} \%THD_i &= 100 \times \frac{I_{dis}}{I_{s1}} \\ &= 100 \times \frac{\sqrt{I_s^2 - I_{s1}^2}}{I_{s1}} \\ &= 100 \times \sqrt{\sum_{h \neq 1} \left(\frac{I_{sh}}{I_{s1}} \right)^2} \end{aligned}$$

Power factor

$$\begin{aligned} PF &= \frac{P}{S} \\ PF &= \frac{V_s I_{s1} \cos \phi_1}{V_s I_s} = \frac{I_{s1}}{I_s} \cos \phi_1 \end{aligned}$$

Crest factor

$$CF = \frac{I_p}{I_{rms}}$$

Power

$$\begin{aligned} P &= \frac{1}{T_1} \int_0^{T_1} p(t) dt = \frac{1}{T_1} \int_0^{T_1} v_s(t) i_s(t) dt \\ &\text{We assume that the voltage} \\ &\text{is pure sinusoidal} \\ P &= \frac{1}{T_1} \int_0^{T_1} \sqrt{2} V_s \sin \omega_1 t \cdot \sqrt{2} I_{s1} \sin(\omega_1 t - \phi_1) dt = V_s I_{s1} \cos \phi_1 \\ S &= V_s I_s \quad \text{(Apparent power)} \end{aligned}$$

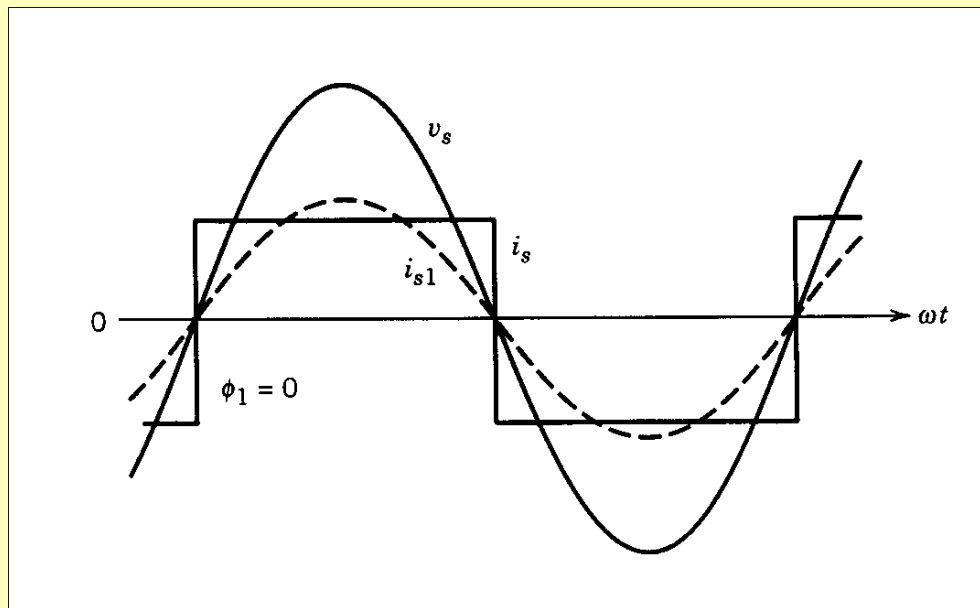
Displacement power factor

$$\begin{aligned} DPF &= \cos \phi_1 \\ PF &= \frac{I_{s1}}{I_s} DPF \\ PF &= \frac{1}{\sqrt{1 + THD_i^2}} DPF \end{aligned}$$

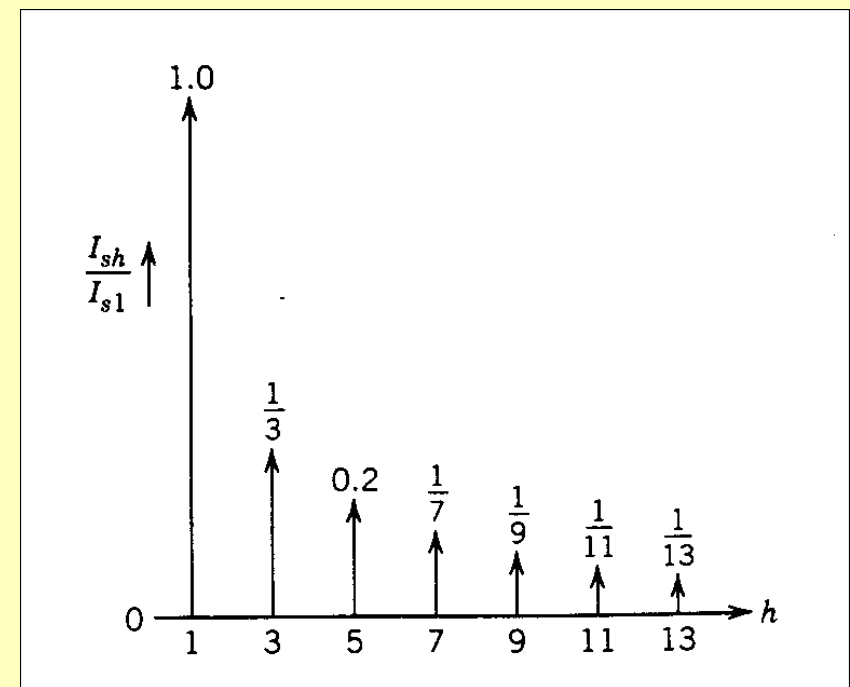
4. Single phase rectifier

Analysis

Fourier analysis



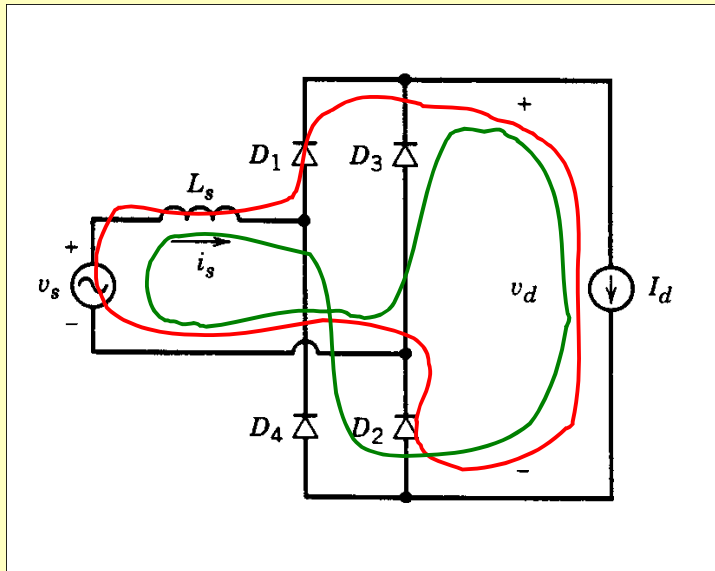
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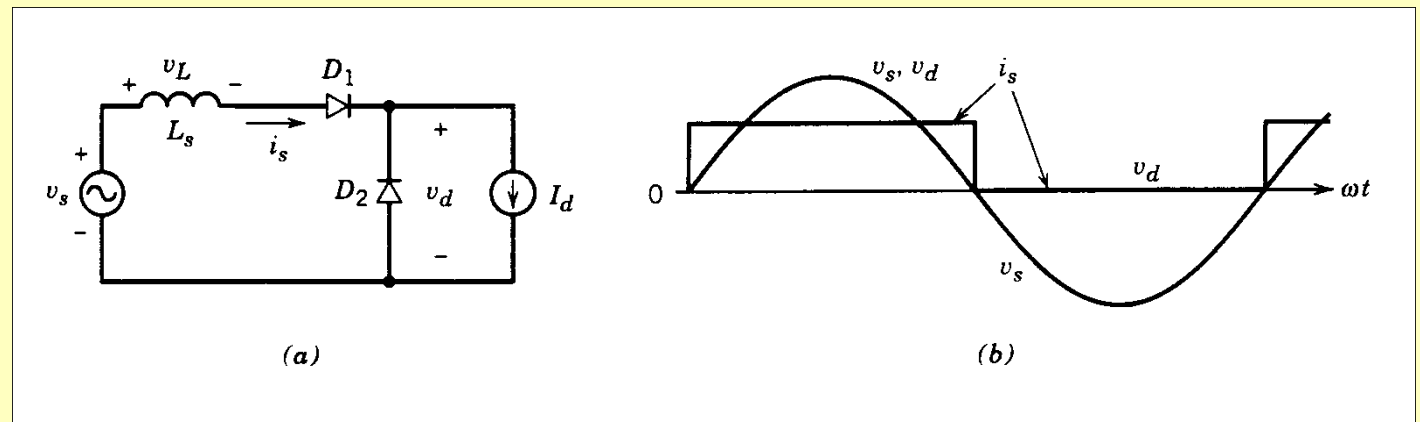
$$THD = 100 \cdot \frac{I_{dis}}{I_{s1}} = 100 \cdot \sqrt{\left(\frac{1}{3}\right)^2 + \left(\frac{1}{5}\right)^2 + \left(\frac{1}{7}\right)^2 + \dots} = 48 \%$$

5. Commutation

Ideal operation ($L_s = 0$)

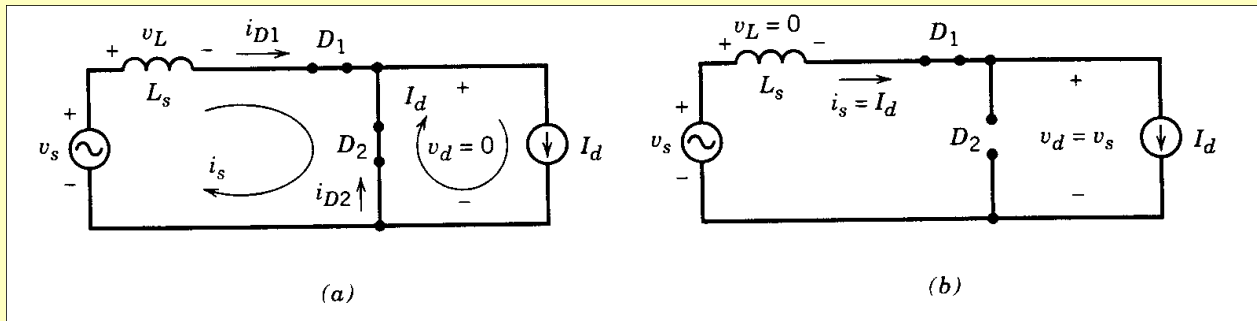


Simplified



5. Commutation

Non-ideal operation ($L_s \neq 0$)



$$A_u = \int_0^u \sqrt{2} V_s \sin(\omega t) d(\omega t) = \omega L_s \int_0^{I_d} di_s$$

Commutation angle

Found from

$$\cos u = 1 - \frac{\omega L_s I_d}{\sqrt{2} V_s}$$

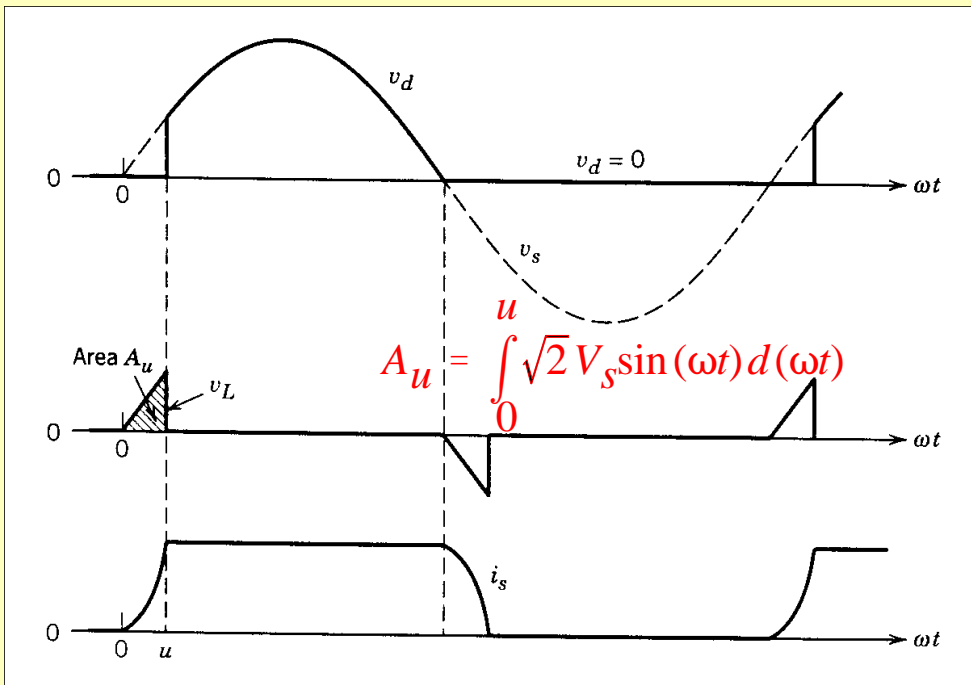
Ideal average voltage

$$V_{do} = \frac{1}{2\pi} \int_0^\pi \sqrt{2} V_s \sin \omega t d(\omega t) = \frac{2\sqrt{2}}{2\pi} V_s = 0.45 V_s$$

Non-ideal average voltage

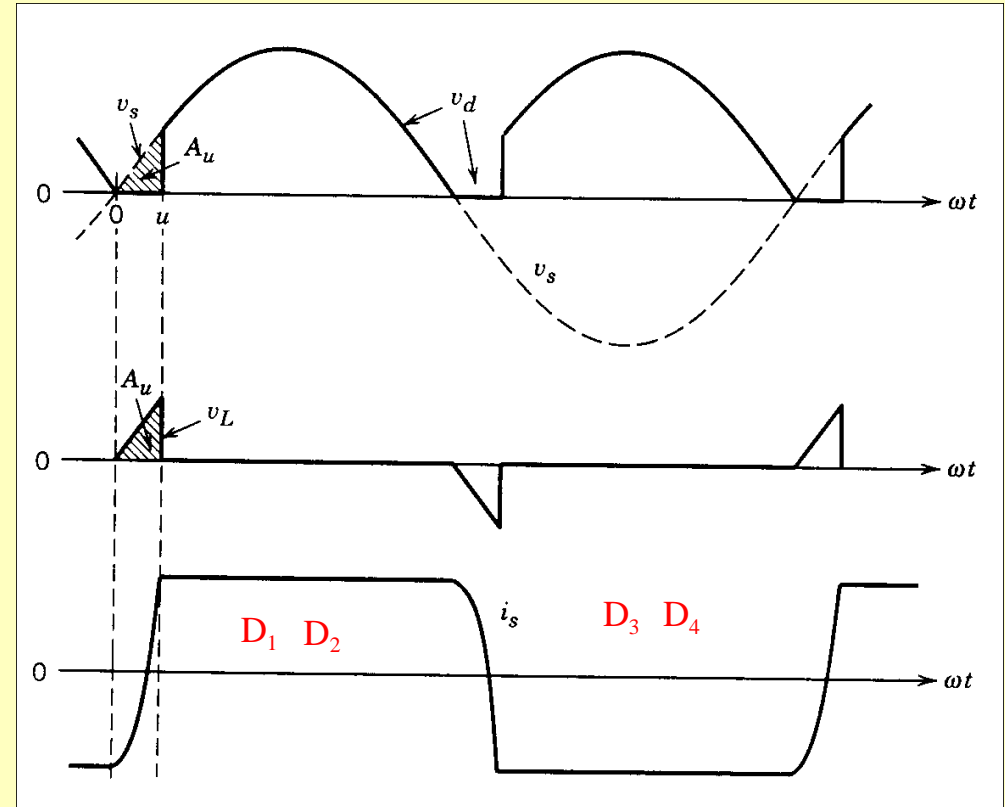
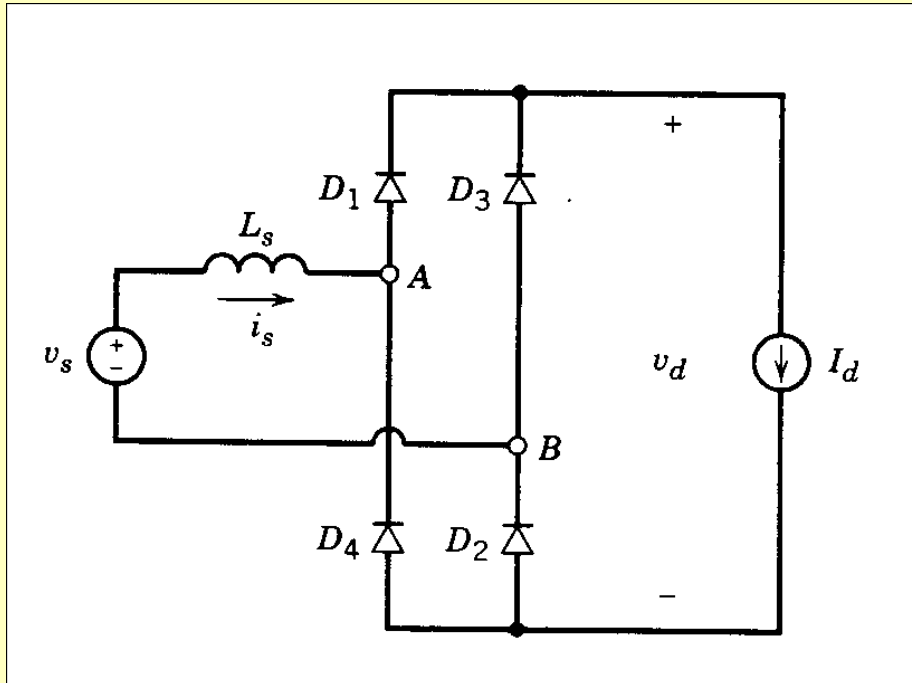
$$V_d = 0.45 V_s - \frac{\text{area } A_u}{2\pi} = 0.45 V_s - \frac{\omega L_s}{2\pi} I_d$$

Reduction in output voltage



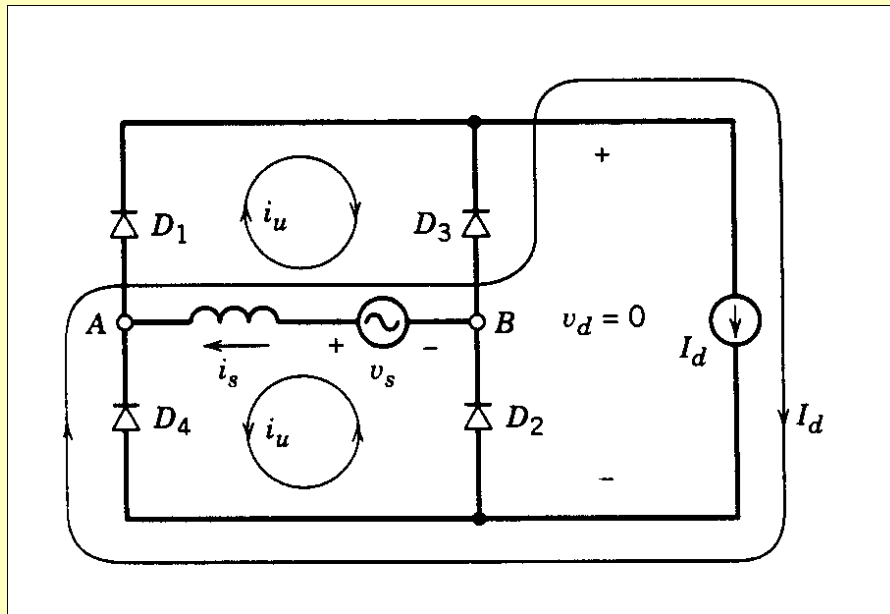
5. Commutation

Full-bridge



5. Commutation

Full-bridge



Average voltage

$$V_d = V_{do} - \frac{\text{area } A_u}{\pi} = 0.9 V_s - \frac{2\omega L_s I_d}{\pi}$$

Same procedure at last method ($-I_d \rightarrow I_d$)

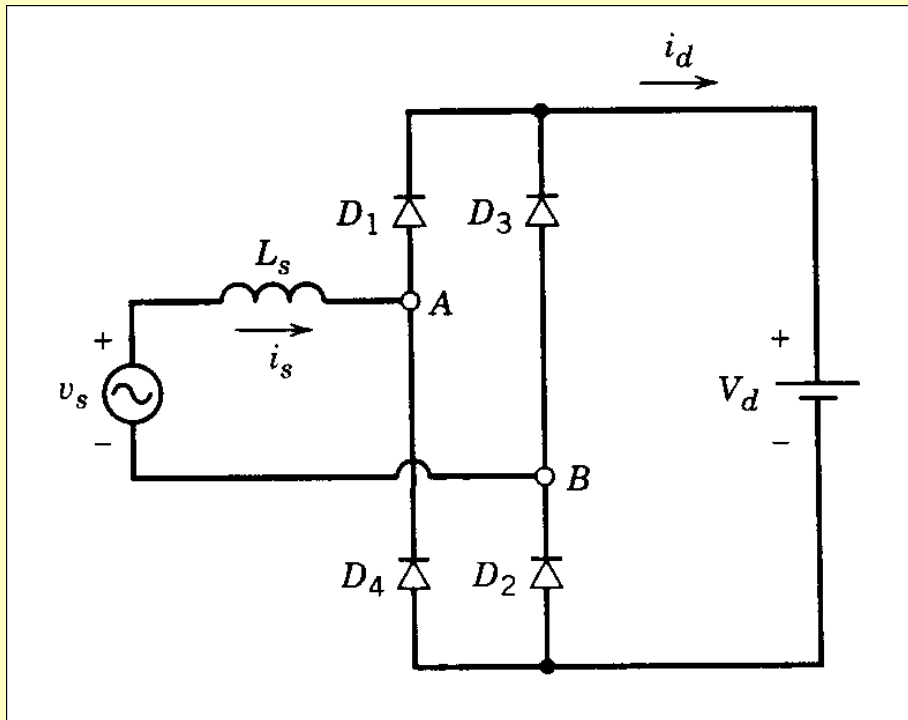
L_s large \Rightarrow Large reduction in voltage

Twice as before

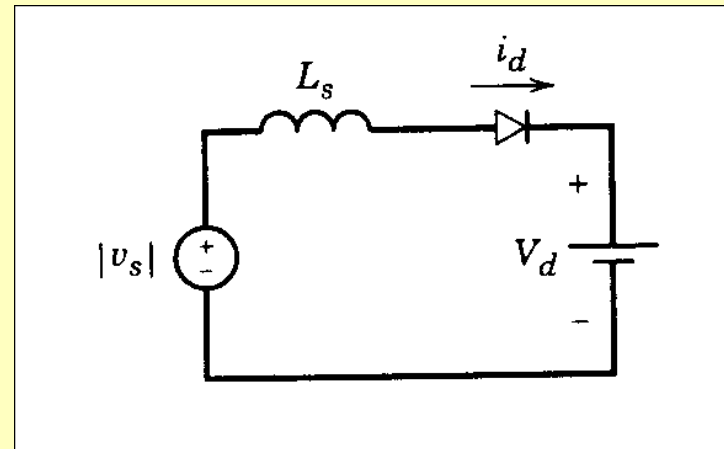
$$\cos u = 1 - \frac{2\omega L_s I_d}{\sqrt{2} V_s}$$

6. Constant DC-link voltage

Circuit



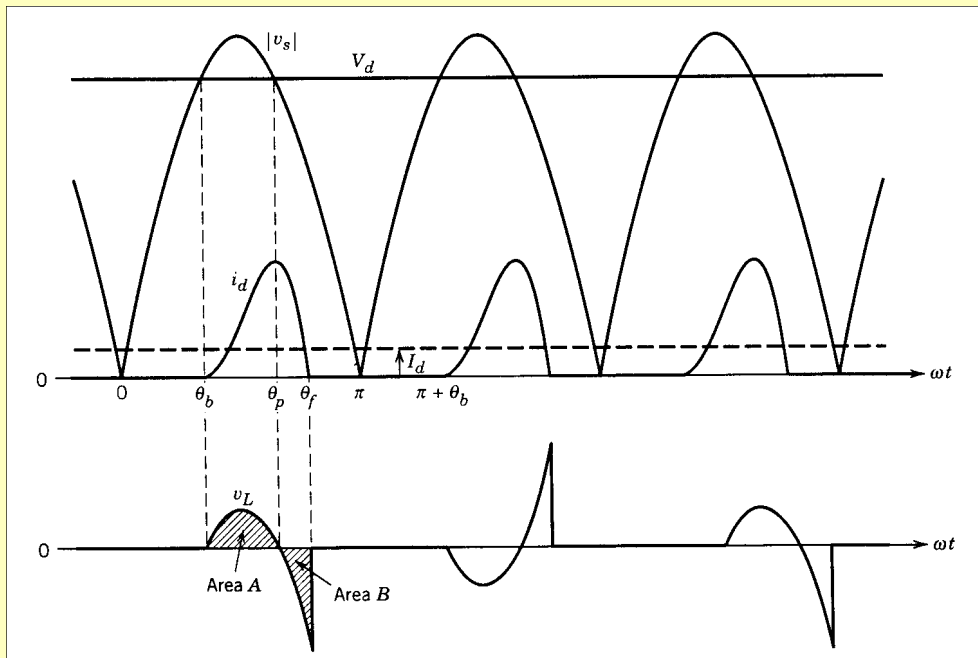
Equivalent



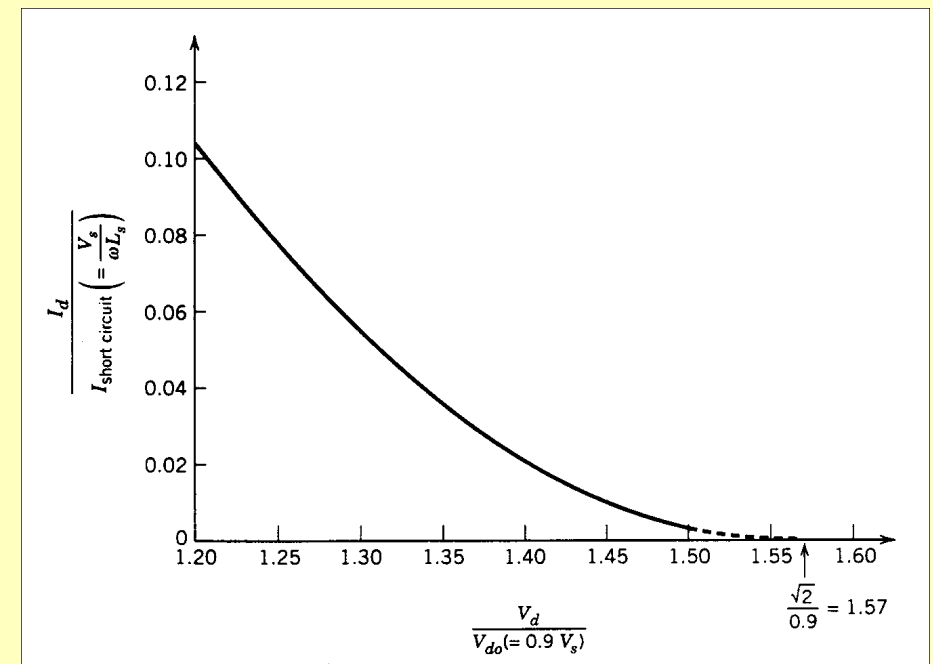
$$I_{\text{short circuit}} = ?$$

6. Constant DC-link voltage

Curves

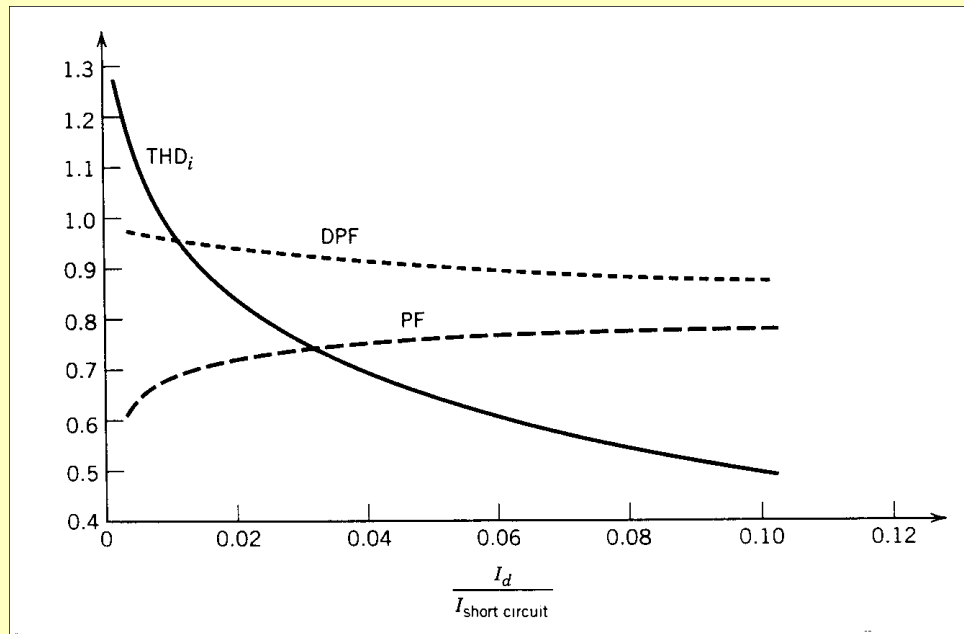


Load current against voltage

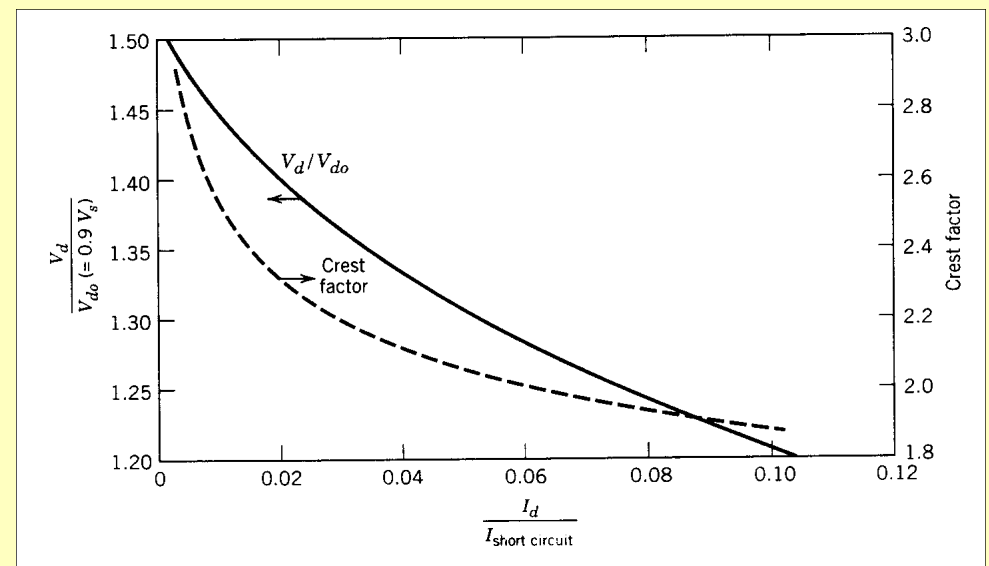


7. Characteristics

Harmonics

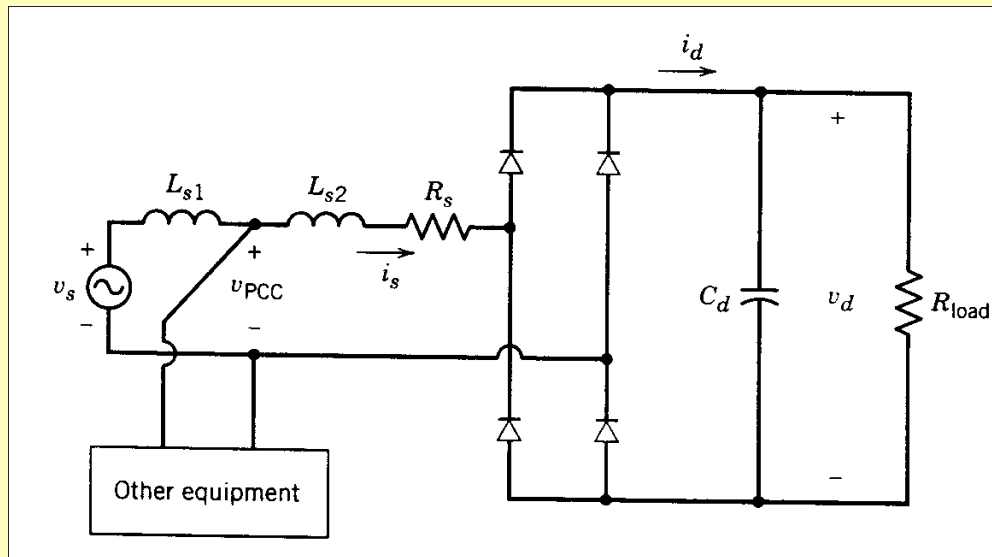


Crest factor

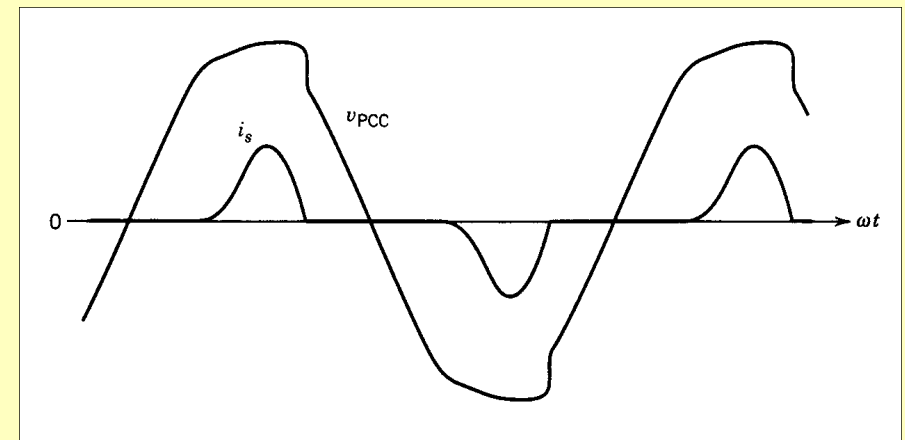


7. Characteristics

Line connected



Curves with line connection



8. Exercises

Exercises

Exercise 5.11

Simulation in PSpice

Exercise 5.14